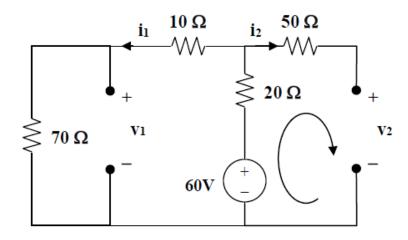
HW 6 Solution

Solution 6.13

Under dc conditions, the circuit becomes that shown below:



$$i_2 = 0$$
, $i_1 = 60/(70+10+20) = 0.6 \text{ A}$
 $v_1 = 70i_1 = 42 \text{ V}$, $v_2 = 60-20i_1 = 48 \text{ V}$

Thus,
$$v_1 = 42 V$$
, $v_2 = 48 V$.

In the circuit in Fig. 6.64, let $i_s = 4.5e^{-2t}$ mA and the voltage across each capacitor is equal to zero at t = 0. Determine v_1 and v_2 and the energy stored in each capacitor for all t > 0.

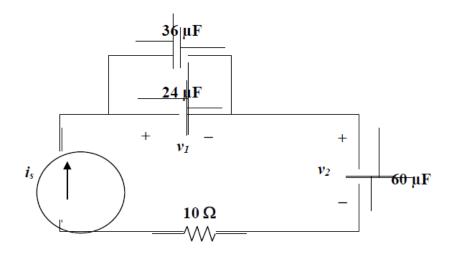


Figure 6.64 For Prob. 6.32.

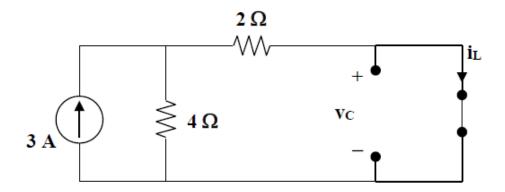
Solution

Combining the 36 μF with the 24 μF we get 60 μF which leads to $v_1 = \frac{1}{60\mu} \int_0^t 4.5e^{-2\tau} m d\tau$ = [37.5–37.5 e^{-2t}] $V = v_2$.

$$(v_1)^2 = \left[(37.5)^2 - 2(37.5)^2 e^{-2t} + (37.5)^2 e^{-4t} \right] = 1406.25 \left[1 - 2e^{-2t} + e^{-4t} \right] = (v_2)^2$$

$$\begin{split} w_{24} &= 0.5x24x10^{-6}(v_1)^2 = \textbf{16.875}[\textbf{1} - \textbf{2}\textbf{e}^{-2\textbf{t}} + \textbf{e}^{-4\textbf{t}}] \ \textbf{mJ} \\ w_{36} &= 0.5x36x10^{-6}(v_1)^2 = \textbf{25.31}[\textbf{1} - \textbf{2}\textbf{e}^{-2\textbf{t}} + \textbf{e}^{-4\textbf{t}}] \ \textbf{mJ} \\ w_{60} &= 0.5x60x10^{-6}(v_2)^2 = \textbf{42.19}[\textbf{1} - \textbf{2}\textbf{e}^{-2\textbf{t}} + \textbf{e}^{-4\textbf{t}}] \ \textbf{mJ} \end{split}$$

Under dc conditions, the circuit is as shown below:



By current division,

$$i_L = \frac{4}{4+2}(3) = 2A, \quad v_c = 0V$$

$$W_{L} = \frac{1}{2}L i_{L}^{2} = \frac{1}{2} \left(\frac{1}{2}\right)(2)^{2} = 1J$$

$$W_c = \frac{1}{2}C \ V_c^2 = \frac{1}{2}(2)(v) = \mathbf{0J}$$

Consider the circuit in Fig. 6.84. Given that $v(t) = 12e^{-3t}$ mV for t > 0 and $i_1(0) = -30$ mA, find: (a) $i_2(0)$, (b) $i_1(t)$ and $i_2(t)$.

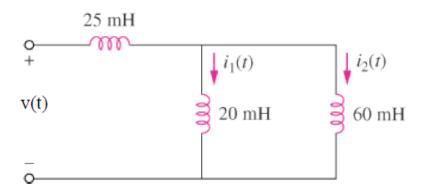


Figure 6.84 For Prob. 6.62.

Solution

(a)
$$L_{eq} = 25 + 20 \parallel 60 = 25 + \frac{20x60}{80} = 40 \text{ mH}$$

 $v = L_{eq} \frac{di}{dt} \longrightarrow i = \frac{1}{L_{eq}} \int v(t)dt + i(0) = \frac{10^{-3}}{40x10^{-3}} \int_{0}^{t} 12e^{-3t}dt + i(0) = -0.1(e^{-3t} - 1) + i(0)$

Using current division and the fact that all the currents were zero when the circuit was put together, we get,

$$i_1 = \frac{60}{80}i = \frac{3}{4}i, \quad i_2 = \frac{1}{4}i$$

 $i_1(0) = \frac{3}{4}i(0) \longrightarrow 0.75i(0) = -0.03 \longrightarrow i(0) = -0.04$

$$i_2 = \frac{1}{4}(-0.1e^{-3t} + 0.06) \text{ A} = (-25e^{-3t} + 15) \text{ mA}$$

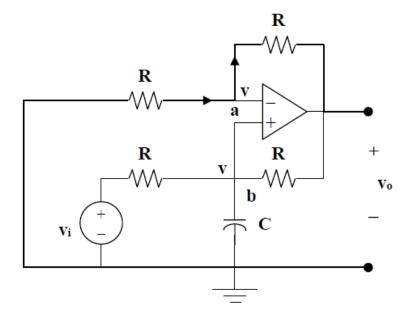
 $i_2(0) = -25 + 15 = -10 \text{ mA}.$

(b)
$$i_1(t) = 0.75(-0.1e^{-3t} + 0.06) = (-75e^{-3t} + 45)$$
 mA and $i_2(t) = (-25e^{-3t} + 15)$ mA.

Consider the op amp as shown below:

Let $v_a = v_b = v$

At node a,
$$\frac{0-v}{R} = \frac{v-v_o}{R}$$
 \longrightarrow $2v-v_o = 0$ (1)



At node b,
$$\frac{V_i - V}{R} = \frac{V - V_o}{R} + C \frac{dV}{dt}$$
$$v_i = 2V - V_o + RC \frac{dV}{dt}$$
 (2)

Combining (1) and (2),

$$v_i = v_o - v_o + \frac{RC}{2} \frac{dv_o}{dt}$$

or

$$v_o = \frac{2}{RC} \int v_i \, dt$$

showing that the circuit is a noninverting integrator.